21MAT01

# ALGEBRA AND CALCULUS (COMMON TO ALL BRANCHES)

| L | T | P | C |
|---|---|---|---|
| 3 | 1 | 0 | 4 |

## **Course Objectives:**

- To provide the skills to the students for solving different real time problems by applying Algebra, matrices and differential calculus.
- Understand the concepts of improper and proper integrals and their applications
- Extend their knowledge of derivatives to find curvature, evolutes, etc., and measure extreme values of a given function of several variables.
- Compute external values which arise in functions of several variables.

## UNIT I ALGEBRA AND MATRICES

12Hours

Inverse and rank of matrices - System of linear equations-Symmetric, Skew symmetric and orthogonal matrices - Unitary matrices-Eigen values and Eigen vectors - Diagonalization of matrices - Cayley-Hamilton Theorem-Reduction from quadratic form to canonical form.

### UNIT II DIFFERENTIAL CALCULUS 12Hours

Curvature of curve - Center and Radius of Curvature (Cartesian polar, parametric and implicit form) Evolutes - Involutes - Envelopes (one parameter and two parameter) - Evolutes as the envelope of normal.

#### UNIT III INTEGRAL CALCULUS 12Hours

Methods of integration-Definite integrals and its properties-Reduction formula for  $e^{ax}x^n$ ,  $\sin^m x$ ,  $\cos^n x$ ,  $\sin^m x \cos^n x$  (without proof) - Problems of Beta and Gamma functions - Inter-relation.

## UNIT IV APPLICATIONS OF DIFFERENTIAL CALCULUS & INTEGRAL CALCULUS

12Hours

Applications of differential calculus -Tangent & Normal –Angle of intersection of two curves – Angle between tangents - Velocity and acceleration - Applications of Integral calculus - Area and Volume in Cartesian and polar coordinates

#### UNIT V FUNCTIONS OF SEVERAL VARIABLES 12Hours

Limits and continuity - partial derivatives -Total derivatives-differentiation of implicit functions - Jacobian - properties of Jacobians - Taylor's series for functions two variables - Maxima and Minima of functions of two variables (proofs of theorems are not included) - Constrained Maxima and Minima-Lagrange's method of multipliers.

#### **Course Outcomes:**

- After the completion of the course the student will be able to
- Solve engineering problems which needs matrix computations.
- Concept of Eigen values and eigenvectors and to reduce the quadratic form to canonical form.
- Identify Radius, Centre, Envelope and circle of curvature and apply them in the problem solving.
- Evaluation of improper integrals using beta and gamma functions
- Apply the concepts in solving physical problems arising in engineering

• Students should be able to apply the basic concepts of differential calculus to solve problems released function to maxima and minima of a single and two variables.

## **Text Books:**

- B.S.Grewal . "Higher Engineering Mathematics", Khanna Publishers, New Delhi, 43rd edition, 2014.
- James Stewart, "Calculus: Early Transcendentals", Cengage Learning, 7th Edition, New Delhi,
  2015
- Thomas' Calculus, George B. Thomas, D. Weir and J. Hass, 13th edition, Pearson, 2014.
- N.P. Bali, "A Text Book of Engineering Mathematics", 13th edition.

#### **References:**

- 1. Jain R.K. and Iyengar S.R.K., "Advanced Engineering Mathematics", Narosa Publications, New Delhi, 3rd Edition, 2007.
- 2. Narayanan, S. and Manicavachagom Pillai, T. K., "Calculus" Volume I and II, S. Viswanathan Publishers Pvt. Ltd., Chennai, 2007.
- 3. Srimantha Pal and Bhunia, S.C, "Engineering Mathematics" Oxford University Press, 2015.

## **Reference Links:**

https://nptel.ac.in > courses https://en.wikipedia.org